M.E. Mechanical Engineering - First Year - Second Semester Examination-2024-25

Sub : Reliability Engineering in Design;

Full Marks : 100 time : 3 hrs

Answer any five questions (20 X5 = 100)

1. a) Define reliability and explain the role of reliability engineering throughout the product life cycle.

   b) Define and derive the expression for

   i) Reliability ii) MTTF iii) B_{20} (the 20th percentile) life

   c) The hazard rate of a component is :

$$h(t) = 0.03t^{1.5}, \quad t \geq 0$$

   The failure rate is in failures per year.

   (i) What is the reliability function of this component and what is the value of the reliability for a period of 2 years?

   (ii) What is the median life or B_{50} life of this component?

6 + 6 + 8

2. a) The no. of days to Failure of 10 components are as follows

1200, 807, 1330, 950, 1055, 1185, 880, 1210, 1395, 1090

Assume two parameter Weibull distribution and estimate the values of failure parameters using analytical method. Calculate the reliability and failure rate of the component for a specific time period of 1025 days.

b) A component has the normal distribution for time to failure, with μ = 26,000 hours and σ = 3500 hours.

(i) Find the probability that the component will fail between 22,000 hours and 23,000 hours.

(ii) Find the failure rate of a component that has been working for 22,000 hours.

10 +10

3. a) Explain the Bath tub curve.

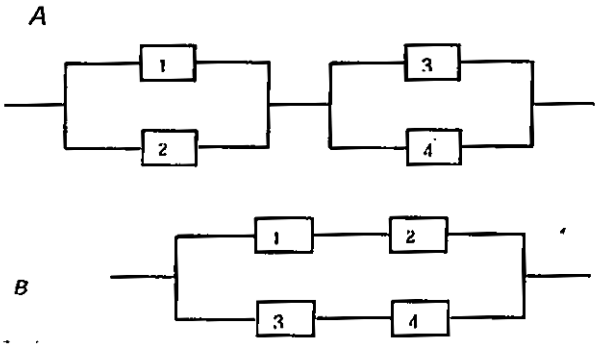
b) What is series configuration? A ten-component system with 95% reliability is to be designed. The system is to be designed in such a way that if any component fails the system would fail. What should be the reliability(R) of each component?

c) In an electrical distribution system, electronically operated circuit breakers(CBs) can be activated to interrupt the current. If the current exceeds 105% of the rated line current it is required that the circuit breakers open, thereby disconnecting the supply. The probability that a circuit breaker functions correctly is 0,98, and each breaker has its own line voltage sensor. If the reliability associated with interrupting the circuit is to be at least 0.999, how many circuit breakers in series are necessary to achieve the desired reliability?

5+7+8

4. a) Explain the 1-Active redundant, 2-Standby redundant and 3-Shared parallel configuration?

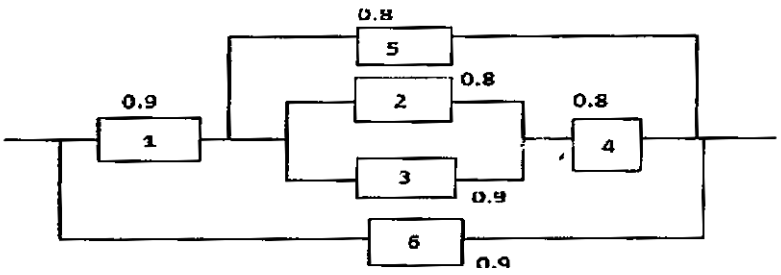
b) let $R_1 = 0.95$, $R_2 = 0.85$, $R_3 = 0.75$, $R_4 = 0.8$ and the components work independent of each other. Calculate the reliability of the configuration.



c) Find out reliability of K-out-n configuration.

6+8+6

5. a) Calculate the reliability of the system shown using network reduction technique?



b) What is Quality Function Deployment? Why it is important ?

c) Design a House of Quality for a Refrigerator/Car/Motor Bike/ A.C machine

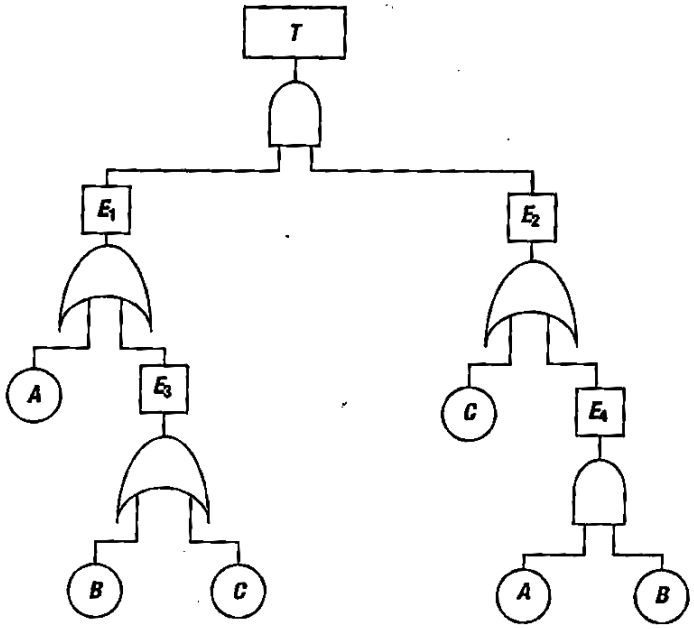
6+6+8

6. Explain the working principle of the optimization techniques (any two)

a) What is Design for Six Sigma ? Why it is important ? Explain the different steps in DFSS .

b)

Analyze the following fault tree:

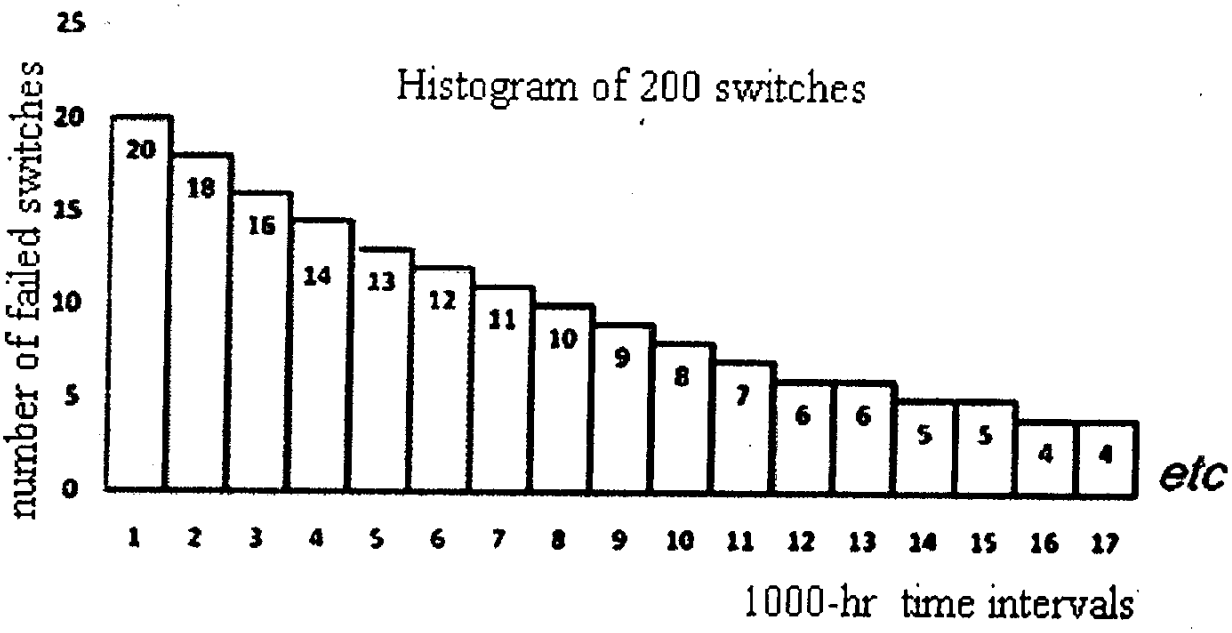


c) Prove that, if the hazard function is constant , the lifetime is exponentially distributed.

10+6+4

7. a) Compare parametric and Non-parametric reliability analysis.

b) . Estimate the density function, the reliability function and the rate function related to a product whose life test results for 200 units are shown on the following histogram.



c) Explain the principle of maximum likelihood.

. Given a random sample X_1 X_1, X_2, X_3, X_n from an exponential distribution, use MLE method to estimate mean.

If the sample is (1.1, 0.9, 1.21, 0.8) calculate the value of mean.

4+8+8

8. a) Explain **accelerated life test** in detail.

b) List and briefly explain the four main assumptions that must hold for a one-way ANOVA to be valid?

Two fatigue life test experiments are done at two different labs on the same material and fatigue strength obtaines as

Test 1 : 540, 560, 532, 546 in MPa

Test 2 : 520, 530, 560, 543 in MPa

Use ANOVA method to conclude whether both materials are same or not ? 8+12

F - Distribution ($\alpha = 0.01$ in the Right Tail)

df_2 \ df_1	1	2	3	4	5	6	7	8	9
	Numerator Degrees of Freedom								
1	4052.2	4999.5	5403.4	5624.6	5763.6	5859.0	5928.4	5981.1	6022.5
2	98.503	99.000	99.166	99.249	99.299	99.333	99.356	99.374	99.388
3	34.116	30.817	29.457	28.710	28.237	27.911	27.672	27.489	27.345
4	21.198	18.000	16.694	15.977	15.522	15.207	14.976	14.799	14.659
5	16.258	13.274	12.060	11.392	10.967	[illegible]	10.456	10.289	10.158
6	13.745	10.925	9.7795	9.1483	8.7459	8.4661	8.2600	8.1017	7.9761
7	12.246	9.5466	8.4513	7.8466	7.4604	7.1914	6.9928	6.8400	6.7188
8	11.259	8.6491	7.5910	7.0061	6.6318	6.3707	6.1776	6.0289	5.9106
9	10.561	8.0215	6.9919	6.4221	6.0569	5.8018	5.6129	5.4671	5.3511
10	10.044	7.5594	6.5523	5.9943	5.6363	5.3858	5.2001	5.0567	4.9424
11	9.6460	7.2057	6.2167	5.6683	5.3160	5.0692	4.8861	4.7445	4.6315
12	9.3302	6.9266	5.9525	5.4120	5.0643	4.8206	4.6395	4.4994	4.3875
13	9.0738	6.7010	5.7394	5.2053	4.8616	4.6204	4.4410	4.3021	4.1911
14	8.8616	6.5149	5.5639	5.0354	4.6950	4.4558	4.2779	4.1399	4.0297
15	8.6831	6.3589	5.4170	4.8932	4.5556	4.3183	4.1415	4.0045	3.8948
16	8.5310	6.2262	5.2922	4.7726	4.4374	4.2016	4.0259	3.8896	3.7804
17	8.3997	6.1121	5.1850	4.6690	4.3359	[illegible]	3.9267	3.7910	3.6822
18	8.2854	6.0129	5.0919	4.5790	4.2479	4.0146	3.8406	3.7054	3.5971
19	8.1849	5.9259	5.0103	4.5003	4.1708	3.9386	3.7653	3.6305	3.5225
20	8.0960	5.8489	4.9382	4.4307	4.1027	3.8714	3.6987	3.5644	3.4567
21	8.0166	5.7804	4.8740	4.3688	4.0421	3.8117	3.6396	3.5056	3.3981
22	7.9454	5.7190	4.8166	4.3134	3.9880	3.7583	3.5867	3.4530	3.3458
23	7.8811	5.6637	4.7649	4.2636	3.9392	3.7102	3.5390	3.4057	3.2986
24	7.8229	5.6136	4.7181	4.2184	3.8951	3.6667	3.4959	3.3629	3.2560
25	7.7698	5.5680	4.6755	4.1774	3.8550	3.6272	3.4568	3.3239	3.2172
26	7.7213	5.5263	4.6366	4.1400	3.8183	3.5911	3.4210	3.2884	3.1818
27	7.6767	5.4881	4.6009	4.1056	3.7848	3.5580	3.3882	3.2558	3.1494
28	7.6356	5.4529	4.5681	4.0740	3.7539	3.5276	3.3581	3.2259	3.1195
29	7.5977	5.4204	4.5378	4.0449	3.7254	3.4995	3.3303	3.1982	3.0920
30	7.5625	5.3903	4.5097	4.0179	3.6990	3.4735	3.3045	3.1726	3.0665
40	7.3141	5.1785	4.3126	3.8283	3.5138	3.2910	3.1238	2.9930	2.8876
60	7.0771	4.9774	4.1259	3.6490	3.3389	3.1187	2.9530	2.8233	2.7185
120	6.8509	4.7865	3.9491	3.4795	3.1735	2.9559	2.7918	2.6629	2.5586
∞	6.6349	4.6052	3.7816	3.3192	3.0173	2.8020	2.6393	2.5113	2.4073

Denominator Degrees of Freedom

Alpha = .05	1	2	3	4	5	6	7	8	9	10
1	161.4476	199.5000	215.7073	224.5832	230.1619	233.9860	[illegible]	238.8827	240.5433	241.8817
2	18.5128	19.0000	19.1643	19.2468	19.2964	19.3295	19.3532	19.3710	19.3848	19.3959
3	10.1280	9.5521	9.2766	9.1172	9.0135	8.9406	8.8867	8.8452	8.8123	8.7855
4	7.7086	6.9443	6.5914	6.3882	6.2561	6.1631	6.0942	6.0410	5.9988	5.9644
5	6.6079	5.7861	5.4095	5.1922	5.0503	4.9503	4.8759	4.8183	4.7725	4.7351
6	5.9874	5.1433	4.7571	4.5337	4.3874	4.2839	4.2067	4.1468	4.0990	4.0600
7	5.5914	4.7374	4.3468	4.1203	3.9715	3.8660	3.7870	3.7257	3.6767	3.6365
8	5.3177	4.4590	4.0662	3.8379	3.6875	3.5806	3.5005	3.4381	3.3881	3.3472
9	5.1174	4.2565	3.8625	3.6331	3.4817	3.3738	3.2927	3.2296	3.1789	3.1373
10	4.9646	4.1028	3.7083	3.4780	3.3258	3.2172	3.1355	3.0717	3.0204	2.9782
11	4.8443	3.9823	3.5874	3.3567	3.2039	3.0946	3.0123	2.9480	2.8962	2.8536
12	4.7472	3.8853	3.4903	3.2592	3.1059	2.9961	2.9134	2.8486	2.7964	2.7534
13	4.6672	3.8056	3.4105	3.1791	3.0254	2.9153	2.8321	2.7669	2.7144	2.6710
14	4.6001	3.7389	3.3439	3.1122	2.9582	2.8477	2.7642	2.6987	2.6458	2.6022
15	4.5431	3.6823	3.2874	3.0556	2.9013	2.7905	2.7066	2.6408	2.5876	2.5437
16	4.4940	3.6337	3.2389	3.0069	2.8524	2.7413	2.6572	2.5911	2.5377	2.4935
17	4.4513	3.5915	3.1968	2.9647	2.8100	2.6987	2.6143	2.5480	2.4943	2.4499
18	4.4139	3.5546	3.1599	2.9277	2.7729	2.6613	2.5767	2.5102	2.4563	2.4117
19	4.3807	3.5219	3.1274	2.8951	2.7401	2.6283	2.5435	2.4768	2.4227	2.3779
20	4.3512	3.4928	3.0984	2.8661	2.7109	2.5990	2.5140	2.4471	2.3928	2.3479
21	4.3248	3.4668	3.0725	2.8401	2.6848	2.5727	2.4876	2.4205	2.3660	2.3210
22	4.3009	3.4434	3.0491	2.8167	2.6613	2.5491	2.4638	2.3965	2.3419	2.2967
23	4.2793	3.4221	3.0280	2.7955	2.6400	2.5277	2.4422	2.3748	2.3201	2.2747
24	4.2597	3.4028	3.0088	2.7763	2.6207	2.5082	2.4226	2.3551	2.3002	2.2547
25	4.2417	3.3852	2.9912	2.7587	2.6030	2.4904	2.4047	2.3371	2.2821	2.2365
26	4.2252	3.3690	2.9752	2.7426	2.5868	2.4741	2.3883	2.3205	2.2655	2.2197
27	4.2100	3.3541	2.9604	2.7278	2.5719	2.4591	2.3732	2.3053	2.2506	2.2043
28	4.1960	3.3404	2.9467	2.7141	2.5581	2.4453	2.3593	2.2913	2.2360	2.1900
29	4.1830	3.3277	2.9340	2.7014	2.5454	2.4324	2.3463	2.2783	2.2229	2.1768
30	4.1709	3.3158	2.9223	2.6896	2.5336	2.4205	2.3343	2.2662	2.2107	2.1646
40	4.0847	3.2317	2.8387	2.6060	2.4495	2.3359	2.2490	2.1802	2.1240	2.0772
60	4.0012	3.1504	2.7581	2.5252	2.3683	2.2541	2.1665	2.0970	2.0401	1.9926
120	3.9201	3.0718	2.6802	2.4472	2.2899	2.1750	2.0868	2.0164	1.9588	1.9105
INF	3.8415	2.9957	2.6049	2.3719	2.2141	2.0986	2.0096	1.9384	1.8799	1.8307